



segments.lines.planes.geometric formulas

GEOMETRY HISTORY

Geometry means earth measurement. Early people used their knowledge of geometry to build roads, pyramids, and irrigation systems. The more formal study of geometry today is based on an interest in logical reasoning and relationships rather than in measurement alone. Euclid (300B.C.) organized Greek geometry into a 13-volume set of books named The Elements, in which the geometric relationships were derived through deductive reasoning. Thus, the formal geometry studied today is often called Euclidean Geometry. This geometry is also called plane geometry because the relationships deal with flat surfaces. Geometry has undefined terms, defined terms, postulates (assumptions that have not been proven, but have "worked" for thousands of years), and theorems (relationships that have been mathematically and logically proven).

GEOMETRIC FORMULAS

Perimeter: The perimeter, P, of a two-dimensional shape is the sum of all side lengths; Area: The area, A, of a two-dimensional shape is the number of square units that can be put in the region enclosed by the sides; (Note: Area is obtained through some combination of multiplying heights and bases, which always form 90° angles with each other, except in circles); Volume: The volume, V, of a 3-dimensional shape is the number of cubic units that can be put in the region enclosed by all the sides

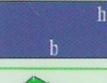
Square Area:

A=hb; if h=8 and b=8 also, as all sides are equal in a square, then: A=64 square units

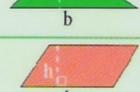
Rectangle Area:

Triangle Area:

A=hb, or A=lw; if h=4 and h=12 then: A=(4)(12), A=48 square units

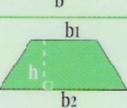


 $A=\frac{1}{2}bh$; if h=8 and b-12 then: $A=\frac{1}{2}(8)(12)$, A=48 square units



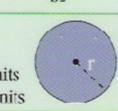
Parallelogram Area: A=hb; if h=6 and b=9 then: A=(6)(9), A=54 square units

Trapezoid Area: $A = \frac{1}{2}h(b_1 + b_2)$; if h=9, b₁=8 and b₂=12 then: $A=\frac{1}{2}(9)(8+12)$, $A=\frac{1}{2}(9)(20)$, A=90 square units



Circle Area:

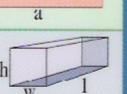
 $A-\pi r^2$; if $\pi-3.14$ and r-5 then: $A=(3.14)(5)^2$, A=(3.14)(25), A=78.5 square units Circumference: $C = 2\pi r$, C = (2)(3.14)(5) = 31.4 units



a and b, then $c^2=a^2+b^2$ Rectangular Prism Volume:

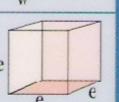
Pythagorean Theorem:

If a right triangle has hypotenuse c and sides



V=lwh; if l=12, w=3 and h=4 then: V=(12)(3)(4), V=144 cubic units

Cube Volume: $V=e^{5}$; each edge length, e, is equal to the other edge in a cube, if e=8 then: V=(8)(8)(8),



Cylinder Volume:

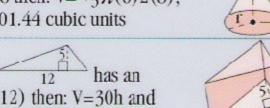
V=512 cubic units

 $V=\pi r^2h$; if radius r=9 and h=8 then: $V=\pi(9)^2(8)$, V=3.14(81)(8), V=2034.72 cubic units



Cone Volume:

 $V=1/3\pi r^2 h$; if r=6 and h=8 then: $V=1/3\pi(6)2(8)$, $V=\frac{1}{3}(3.14)(36)(8)$, V=301.44 cubic units



area equal to $\frac{1}{2}(5)(12)$ then: V=30h and if h=8 then: V=(30)(8), V=240 cubic units

Triangular Prism Volume:

V=(area of triangle)h; if

Rectangular Pyramid Volume: $V=\frac{1}{3}$ (area of rectangle)h; if l=5 and w=4the rectangle has an area of 20, then: $V=\frac{1}{3}(20)h$ and if h=9 then: $V=\frac{1}{3}(20)(9)$, V=60 cubic units



Sphere Volume:

 $V = \frac{4\pi r^3}{3}$; if radius r=5 then: $V = 4(3.14)(5)^3$, V = 1570, 523.3 cubic units



DESCRIPTIONS OF UNDEFINED TERMS

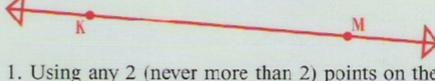
Point

- A. A point may be described as a location with no length, no width, and no depth
- B. A point is always named with a capital letter; it is usually located by using a dot about the size of a period, although true points cannot really be drawn because they have no dimensions

For Example: .A (indicates point A)

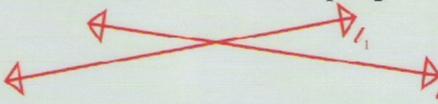
Line

- A. A line may be described as a set of points going straight on forever in two opposite directions; lines are straight and never end; there is never a need to use the phrase "straight line" because lines are straight; if something is not straight it cannot be a line, but might be a curve instead; lines have length, but no width and no depth; lines cannot be truly drawn because they lack width and depth; representations of lines are drawn with arrows at each end indicating that the line has no end
- B. Lines are usually named in one of two ways; the line containing points K and M may be named by either:



1. Using any 2 (never more than 2) points on the line with a line indicator above the points, for example: km or MK (the order of the points doesn't matter); the line indicator above the capital letters always points horizontally from side to side and never any other direction; it is the actual location of the points in space that determines the location and direction of the real line, not the direction of the line indicator above the capital letters in the notation; or

2. By using the lower case script letter / with a number subscript, for example: /1 or /2

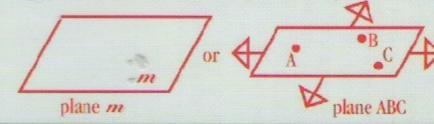


(Note: In coordinate geometry, points can be assigned numbered values, and, as a result, equations of lines can be determined) [See Algebra-Part 2]

Planes

A. A plane may be described as a set of points going on forever in all directions, except any direction that creates depth; imagine the very surface of a perfectly flat piece of paper extending on forever in every direction but having no thickness at all; the result would be a situation such that when any two points in this plane are connected by a line, all points in the line are also in the plane; planes have length and width, but no depth

B. Planes are simply referred to as "plane m" or "plane ABC (any three points on the plane that are not on the same line)" or "the plane containing (whatever pertains to the discussion)"; planes cannot be drawn; representations of planes are usually drawn as parallelograms, either with the arrows indicating that the points go on forever or without the arrows even though the points do go on forever

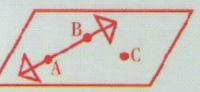


Postulates

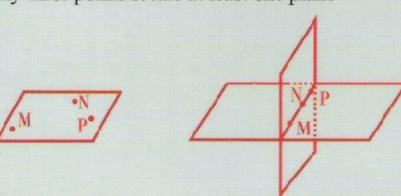
Postulates are statements that have been used and accepted for centuries without formal proof; these are postulates:

A. A line contains at least two points, and any two points locate exactly one line

B. A plane contains at least three points that are not all on the same line, and any three points that are not on the same line locate exactly one plane; therefore, a line and one point not on the line also locate exactly one plane



C. Any three points locate at least one plane



One plane when the three points are not on the same line

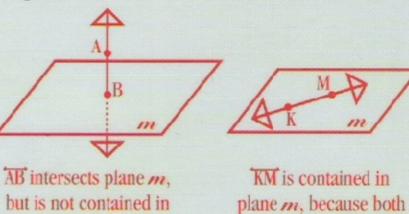
plane m

More than one plane when the three points are on the same line

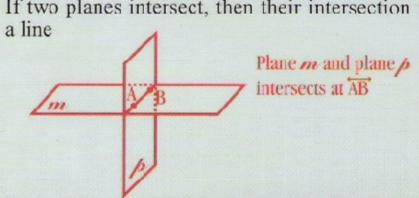
points K and M are in

plane m

D. If two points of a line are in a plane, then the line is in the plane; or, if two points are in a plane, then the line containing the two points is also in the plane



E. If two planes intersect, then their intersection is



DEFINED TERMS

There are many defined terms of plane geometry; the definitions of these terms will be given by topic groups throughout the study guide rather than grouped in one big list

(Note: Postulates (or axioms) are relationships and statements that have worked for centuries and are accepted without mathematical proof; theorems are relationships and statements that have been proven mathematically; postulates and theorems are given throughout this guide; they also are stated under the various topics of geometry; sometimes they are labeled as postulates or theorems, and sometimes they are simply stated and not labeled)

Space

Refers to the set of all points; space goes on forever inevery direction, and therefore has length, width and depth; space has no special notations; it is simply referred to as space; space contains at least four points that are not all on the same plane

General Terms

A. ≅ or congruent shapes are the same shape and size; therefore, after some movement of the shapes they can be made to fit exactly on top of one another

(Note: Corresponding parts of congruent polygons are congruent; that is, once the polygons have been moved around to match up perfectly, then the parts that match (correspond) are congruent)

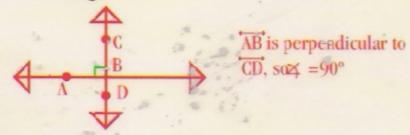
<u>QuickStudy</u>

b. Intersecting lines lie in 1 plane

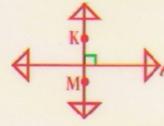
/ 1 and / 2 intersect at point D and lie in plane m

2. Perpendicular Lines

a. Perpendicular lines are lines that intersect and form 90° angles (see the section on angles) at the intersection; the 90° angles are indicated on diagrams by drawing a small square in the corner by the vertex of the angle

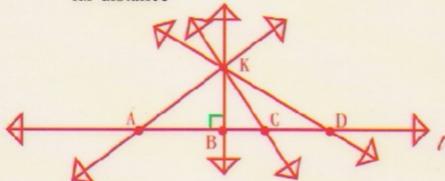


b. Through a point not on a line, exactly one perpendicular can be drawn to the line



If point K is not on \(\mathcal{I}\), then there is exactly 1 line through K that is perpendicular to 1, KM

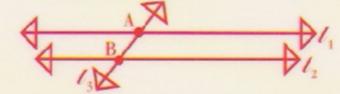
- c. I means "is perpendicular to"; therefore, 11 1 2 is read "line 1 is perpendicular to line 2"
- d. Theorem: The shortest distance from any point to a line or to a plane is the perpendicular distance



The shortest distance from point K to /1 is the distance from K to B

3. Transversal Lines

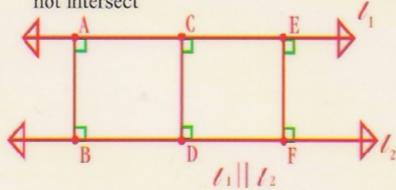
a. A transversal is a line that intersects two or more coplanar lines at different points



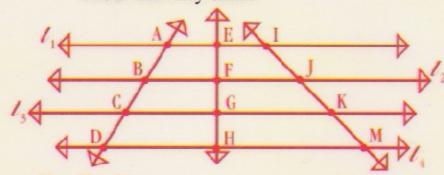
13 is a transversal because it intersects 11 at A and 12 at B

4. Parallel Lines

a. Parallel lines lie in the same plane (coplanar) and share no points in common; i.e., they do not intersect



- b. Parallel lines go in the same directions and never touch; parallel lines are everywhere the same distance apart
- c. Through a point not on a line, exactly 1 parallel can be drawn to the line
- d. means "is parallel to," so $\ell_1 \parallel \ell_2$ is read "line 1 is parallel to line 2"
- e. Theorem: If three or more parallel lines cut off equal segments on 1 transversal, then they cut off equal segments on every transversal that they share



If $l_1 \mid l_2 \mid l_3 \mid l_4$ and if AB = BC = CD, then EF = FG = GHand IJ = JK = KM

Consult angle and line notation for these examples:

Pentagon ABXDE

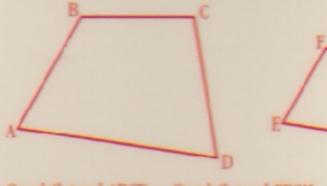
Pentagon RPNMS such that matching sides have equal lengths and matching angles have equal measures; if side $\overline{AB} = 2$ feet then side PR = 2 feet

Corresponding parts are: $\overline{AB} \cong PR$; $\overline{BC} \cong \overline{MP}$; $\overline{CD} \cong \overline{MN}$; $\overline{DE} \cong \overline{MS}$; $\overline{EA} \cong \overline{SR}$; $A \cong A \cong AR$;

4B = 4P.4C = 4N.4D = 4M.4E = 4S

B. ~ or similar shapes are the same shape, but can be different sizes; thus, congruent shapes are also similar shapes, but similar shapes are not necessarily congruent shapes; (Note: two or more similar shapes have corresponding (matching) interior angles of one polygon congruent to the corresponding interior

angles of the other, but the corresponding sides are proportional, not necessarily congruent)



Quadrilateral ABCD ~ Quadrilateral EFGH; therefore, matching angles have equal measures and matching sides have proportional measures For example: If AB = 8 and EF = 4 and BC = 7, then FG = 3.5; that is, $\frac{AB}{EF} = \frac{BC}{FG} = \frac{CD}{GH} = \frac{DA}{HE}$

and $\angle A \cong \angle E$, $\angle B \cong \angle E$, $\angle C \cong \angle G$ and $\angle D \cong \angle H$

C. = or equal can apply to sets of points being exactly the same set or to numerical measurements being exactly the same number values

D. ∪ or union refers to putting all of the points

together and describing the result

E. \(\cap \) or intersection refers to describing only those points that are common to all sets involved in the intersection or to describing the points where indicated shapes touch

Lines

While the word line has no formal definition, there are some particular terms that refer to relationships involving lines:

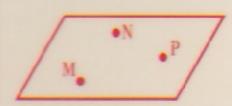
A. Collinear points are points that are on the same



Points A, B and C are collinear

Points D, E and F are noncollinear

B. Noncollinear points are points that are not on the same line; any three noncollinear points are on some plane, however, and so are coplanar

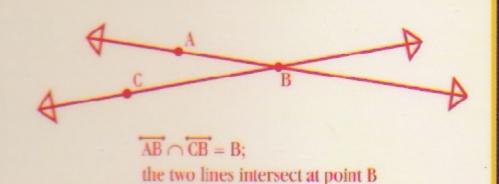


Points M. N and P are noncollinear, but are on the same plane, and so are coplanar

C. Categories of Lines

1. Intersecting Lines

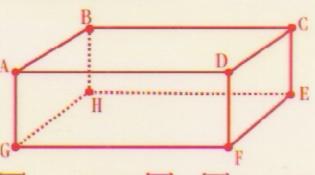
a. Intersecting lines share one and only one point in common



(Note: Special angles that result when two or more lines are intersected by a transversal are discussed *under the topic of angles)*

5. Skew Lines

a. Skew lines are not in the same plane (noncoplanar) and never touch; they go in different directions

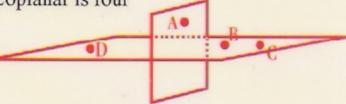


AB and DC are parallel, but AB and GF are skew because they never touch and they go in different directions

Planes

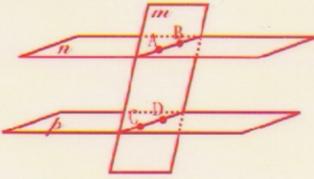
While the word "plane" has no formal definition, the following terms do:

- A. Coplanar means in the same plane; therefore, coplanar points lie in the same plane
- B. Noncoplanar means not in the same plane; three points cannot be noncoplanar because there is some plane that exists that contains any three points; the smallest number of points that can be noncoplanar is four



Points B, C and D are coplanar, but points B, C, D and A are noncoplanar

- C. A line and a plane are parallel if they do not touch or intersect
- D. Two or more planes are parallel if they do not touch or intersect



Planes n and p are parallel; Planes m and n intersect at AB Planes m and b intersect at CD Notice: AB | CD because plane n is parallel to plane p

E. Theorem: If two parallel planes are both intersected by a third plane, then the lines of intersection are parallel

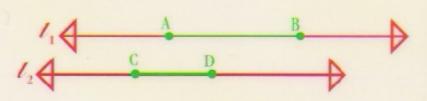
Line Segments

A. A line segment is the set of any two points on a line (the endpoints) and all the collinear points between them; a line segment is named using the two endpoints and a bar notation drawn above these two points; for example, PR includes endpoints P and R and all of the collinear points between them

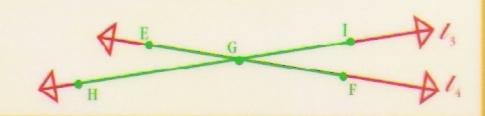
(Note: $\overline{PR} = \overline{RP}$ because both notations name exactly the same set of points)



- B. The union of two line segments depends on the location of each; for example, these conditions could exist:
 - 1. They do not touch: Then $\overline{AB} \cup \overline{CD} = \{all \text{ points}\}$ on \overline{AB} together with all the points on \overline{CD}



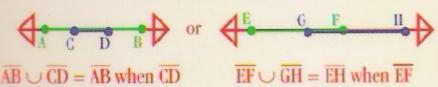
2. They touch in one point: Then $\overline{EF} \cup \overline{HI} =$ {all points on EF together with all of the points on III }



is contained in AB

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3. They touch in more than one point: Then

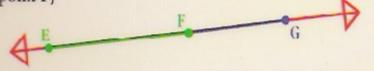


and GH overlap

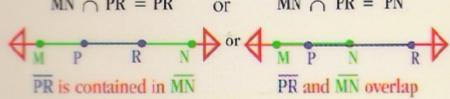
- C. The intersection of two line segments is either no points (they do not touch), one point, or another line segment; for example: these conditions could exist
- 1. They do not touch; then \overline{AB} \cap \overline{CD} = the empty set because they have no points in common \overline{AB} \cap \overline{CD} = \emptyset



2. They touch in one point: Then $\overline{EF} \cap \overline{FG} = \{\text{point } F\}$



3. They touch in more than one point: Then $\overline{MN} \cap \overline{PR} = \overline{PR}$ or $\overline{MN} \cap \overline{PR} = \overline{PN}$



D. The length of a line segment or the distance between two points is a numerical value; the notation for distance is two capital letters with no bars or additional notations above the letters; for example: The distance between point T and point S is indicated by the notation TS with no commas and no additional notations above the two capital letters

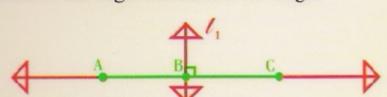
TS means line segment with endpoints T and S
TS means the length of TS

E. The midpoint of a line segment is a point exactly in the middle of the two endpoints; for example: Point R is the midpoint of TS if point R is on TS and TR = RS; also notice that TR + RS = TS



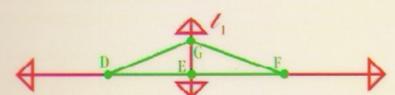
TR = RS so R is the midpoint of \overline{TS}

- F. The bisector of a line segment intersects the line segment at its midpoint; a bisector can be a point, line, line segment, ray, plane, as well as other shapes
- G. The perpendicular bisector of a line segment intersects the line segment at its midpoint and forms 90° angles at the intersection (see the section on angles); a square in the corner by the vertex of the angle indicates a 90° angle



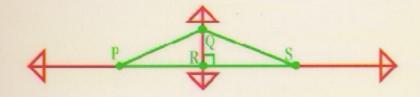
 I_1 is the \perp bisector of \overline{AC} because it forms 90° angles at the midpoint, B, of \overline{AC}

1. Theorem: If a point lies on the perpendicular bisector of a line segment, then the point is equidistant (equal distances) from the endpoints of the line segment



l₁ is the \perp bisector of \overline{DF} so GD = GF, the distance from G to D and G to F are equal

2. **Theorem**: If a point is equidistant from the endpoints of a line segment, then the point lies on the perpendicular bisector of the line segment



If PQ = QS and PR = RS, then \overrightarrow{QR} must be the \bot bisector of \overrightarrow{PS}

H. To **trisect** a line segment, separate it into three other line segments such that the sum of the lengths of the three segments is equal to the length of the original line segment; for example: \overline{AB} has been trisected at points C and D because AC + CD + DB = AB

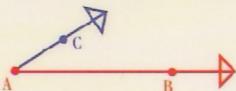


Rays

A. A ray is the set of collinear points going in 1 direction from a point (the endpoint of the ray) on a line; the length of a ray cannot be measured because it has only one endpoint; the notation for writing a ray is two capital letters indicating first, the endpoint of the ray, and second, any other point on the ray; a bar with an arrowhead on the right end must be drawn above the letters to indicate that it is a ray; for example: \overrightarrow{AB} has the endpoint A and goes forever in the direction of point B; however, \overrightarrow{BA} has the endpoint B and goes on forever in the direction of point A; notice that \overrightarrow{AB} and \overrightarrow{BA} do not contain the same set of points, therefore $\overrightarrow{AB} \neq \overrightarrow{BA}$

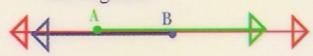


- B. The union or intersection of two rays depends on their relative positions; for example:
 - If the two rays do not touch, the union is simply all the points on both rays, and there is no intersection or common points
 - 2. If the two rays touch in one and only one point, but not at the endpoint, then the union is all the points on both rays, and the intersection is that 1 point where they touch
 - If the two rays touch in one and only one point, the endpoint, then the union is an angle, and the intersection is the endpoint



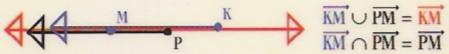
 $\overrightarrow{AB} \cap \overrightarrow{AC} = \angle CAB$ $\overrightarrow{AB} \cap \overrightarrow{AC} = A$

4. If the two rays touch in more than one point, then the union is a line, and the intersection is a line segment

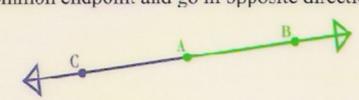


 $\overrightarrow{AB} \cup \overrightarrow{BA} = \overrightarrow{AB}$

or the union is a ray and the intersection is another ray



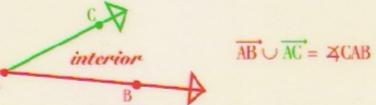
C. Opposite rays are collinear rays that share only a common endpoint and go in opposite directions



 \overrightarrow{AB} and \overrightarrow{AC} are opposite rays because $\overrightarrow{AB} \cup \overrightarrow{AC} = \overrightarrow{CB}$ and $\overrightarrow{AB} \cap \overrightarrow{AC} = \overrightarrow{A}$

Angles

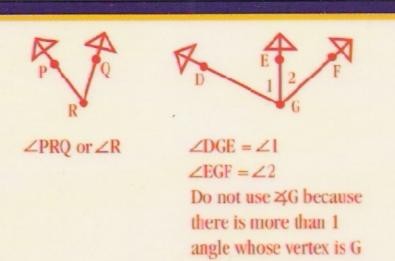
A. An **angle** is the union of two rays that share one and only one point, the endpoint of the rays; the sides of the angle are the rays and the vertex of the angle is the common endpoint of the rays; the interior of the angle is all the points between the two sides of the angle; the plural of vertex is vertices



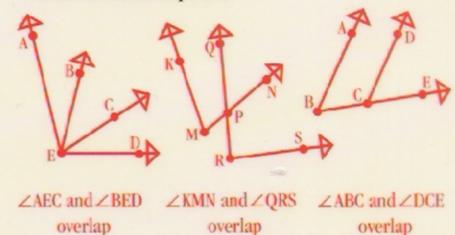
∠ or ∠ are symbols that are read "angle"

Notice that the symbols are both flat on the bottom, unlike the "less than" symbol <

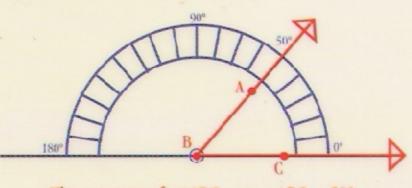
An angle may be named using the vertex only if there is only one angle at the vertex; if more than one angle is present at the vertex, then the angle must be named by either using three points of the angle, with the vertex listed as the middle letter, or by assigning the angle a numerical name in the interior of the angle, close to the vertex



B. Overlapping angles are angles that share some common interior points

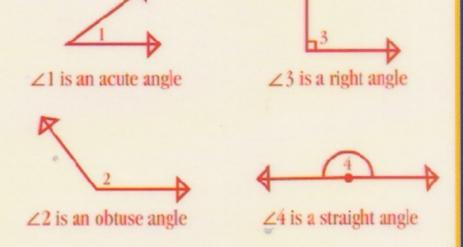


C. Angles are **measured** using a protractor and degree measurements; there are 360° in a circle; placing the center of a protractor at the vertex of an angle and counting the degree measure is like putting the vertex of the angle at the center of a circle and comparing the angle measure to some of the degrees of the circle

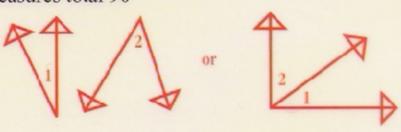


The measure of \angle ABC = m \angle ABC = 50° Notice: m \angle ABC means the measure of the angle in degrees

- D. An acute angle is an angle that measures less than 90°
- E. An **obtuse** angle is an angle that measures more than 90° degrees
- F. A right angle is an angle that measures exactly 90°; it is indicated on diagrams by drawing a square in the corner by the vertex of the angle
- G. A straight angle is an angle that measures exactly 180°

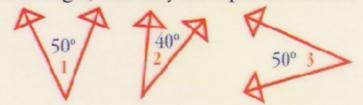


H. Complementary angles are 'wo angles whose measures total 90°



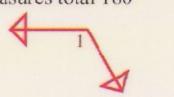
m $\angle 1 = 30^{\circ}$ and $\angle 2 = 60^{\circ}$, so $\angle 1$ and $\angle 2$ are copleentary angles

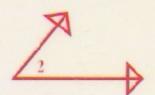
1. **Theorem**: If two angles are complements of the same angle, then they are equal in measure



 $\angle 1$ and $\angle 2$ are complements, $\angle 2$ and $\angle 3$ are complements, therefore, m $\angle 1$ = m $\angle 3$ = measurements

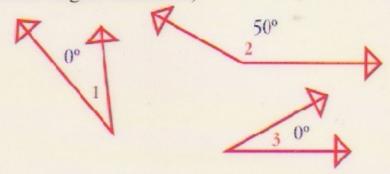
Theorem: If two angles are complements of congruent angles (angles having the same degree measures), then they are congruent





 $m\angle 1 = 120^{\circ}$ and $m\angle 2 = 60^{\circ}$, so $\angle 1$ and $\angle 2$ are supplementary angles because $m\angle 1 + m\angle 2 = 180^{\circ}$

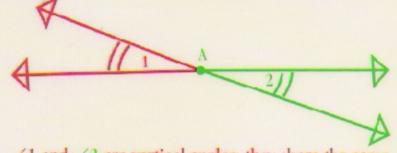
1. Theorem: If two angles are supplements of the same angle, then they are congruent (have the same degree measures)



 $\angle 1$ and $\angle 2$ are supplements; $\angle 2$ and $\angle 3$ are supplements, therefore, $m\angle 1 = m\angle 3$; $\angle 1 \cong \angle 3$

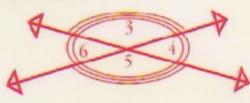
- 2. Theorem: If two angles are supplements of congruent angles, then they are congruent
- J. Vertical angles are two angles that share only a common vertex and whose sides form lines

 Note: Angles with equal measures are indicated by equal number of curves in the angle interiors



 $\angle 1$ and $\angle 2$ are vertical angles; they share the same vertex, Λ , and their sides form lines; $m\angle 1 = m\angle 2$

1. Theorem: Vertical angles are congruent and have equal measures



 $\angle 3$ and $\angle 5$ are vertical angles; m $\angle 3$ = m $\angle 5$

 $\angle 6$ and $\angle 4$ are vertical angles; $m\angle 6 = m\angle 4$

∠4 and ∠5 are supplements

∠5 and ∠6 are supplements

∠6 and ∠3 are supplements

 $\angle 3$ and $\angle 4$ are supplements

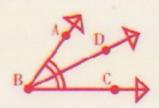
K. Adjacent angles are two angles that share exactly one vertex and one side, but no common interior points; i.e., they do not overlap



∠ABC and ∠CBD are adjacent ∠s
∠ABC ∩ ∠CBD = BC

But ∠ABD and ∠CBD are not
adjacent angles because they
share common interior points
and overlap

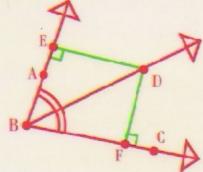
L. An angle is **bisected** by a ray or a line that contains the vertex of the angle, is in the interior of the angle, and separates the angle into two adjacent angles with equal measures



BD bisects∠ ABC
because m∠ABD = m∠DBC and
∠ABD and∠ DBC are adjacent

1. Theorem: If a point lies on the bisector of an angle, then the point is equidistant (equal distances) from the sides of the angle

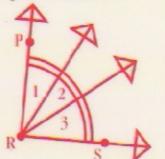
(Note: Distance from a point to a line is always measured on the perpendicular line segment that connects the point and the line)



ED = FD because D is on \overline{BD} which bisects $\angle ABC$

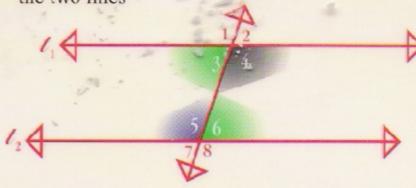
2. Theorem: If a point is equidistant (equal distances) from the sides of an angle, then the point lies on the bisector of the angle

M. An angle is trisected by rays or lines that contain the vertex of the angle and separate the angle into three adjacent angles (in pairs) that all have equal measures



 \angle PRS is trisected because m \angle 1 = m \angle 2 = m \angle 3, and angles 1, 2 and 3 do not overlap

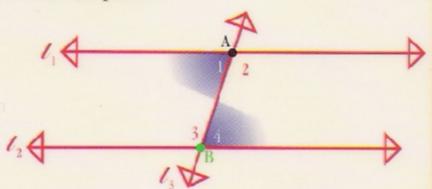
- N. Angles formed when two or more lines are intersected by a transversal:
 - 1. Interior angles are formed with the rays from the two lines and the transversal such that the interior regions of the angles are between the two lines



Angles 3, 4, 5 and 6 are interior angles Angles 1, 2, 7 and 8 are exterior angles

 Alternate interior angles are two interior angles that have different vertices and are on opposite sides of the transversal

Theorem: If the lines are parallel, then the alternate interior angles are equal in measure, and if the alternate interior angles are equal in measure, then the lines are parallel



Angles 1, 2, 3 and 4 are interior angles
Angles 1 and 4 are alternate interior angles because
they have different vertices and are on opposite sides
of the transversal ₹3; ∠1 has vertex A and its interior is
on the left of ₹3; ∠4 has vertex B and its interior is on
the right side of ₹3; Additionally, ∠2 and ∠3
are alternate interior angles

3. Same side interior angles are 2 interior angles that have different vertices and are on the same

side of the transversal

If l_1 and l_2 are parallel, then $\angle 1 = \angle 4$ and $\angle 2 = \angle 3$

 l_2 l_3 l_3 l_3

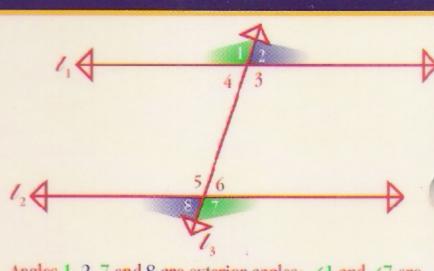
 $\angle 1$ and $\angle 3$ are same side interior angles; they are both on the left side of ℓ_3 and $\angle 1$ has vertex A while $\angle 3$ has vertex B; $\angle 2$ and $\angle 4$ are also same side interior angles

Theorem: If the lines are parallel, then the same side interior angles are **supplementary** (total 180°), and if the same side interior angles are supplementary, then the lines are parallel

If $\ell_1 \mid \mid \ell_2$ above, then $m \angle 1 + m \angle 3 = 180^{\circ}$ and $m \angle 2 + m \angle 4 = 180^{\circ}$

4. Exterior angles are formed when two or more lines are intersected by a transversal; they are formed by the lines and the transversal such that the interior regions of the angles are not between the two lines, but are outside and away from the two lines



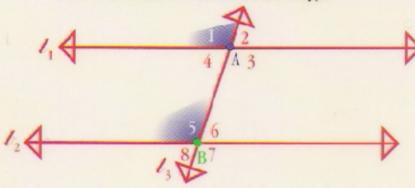


Angles 1, 2, 7 and 8 are exterior angles; $\angle 1$ and $\angle 7$ are alternate exterior angles, as are $\angle 2$ and $\angle 8$

5. Alternate exterior angles are exterior angles that have different vertices and are on opposite sides of the transversal; if the lines are parallel, then the alternate exterior angles are equal in measure, and if the alternate exterior angles are equal in measure, then the lines are parallel

If l_1 and l_2 above are parallel, then $m \angle 1 = m \angle 7$ and $m \angle 2 = m \angle 8$

6. Corresponding angles are angles that have different vertices, are on the same side of the transversal, and are in the same positions relative to the lines and the transversal; one of the pair of corresponding angles is an interior angle and the other is an exterior angle



 $\angle 1$ and $\angle 5$ are corresponding angles; the interior of $\angle 1$ is on the left of $\angle 3$, on top of $\angle 1$, $\angle 1$ has vertex A while $\angle 5$ has vertex B; the interior of $\angle 5$ is also on the left of $\angle 3$ and on top of $\angle 2$; if you slide the 4 angles at vertex B up the transversal, $\angle 3$, to vertex A, then $\angle 5$ would land on $\angle 1$, $\angle 6$ on $\angle 2$, $\angle 7$ on $\angle 3$, and $\angle 8$ on $\angle 4$; so these are all pairs of corresponding angles:

∠1 and ∠5

 $\angle 2$ and $\angle 6$

 $\angle 3$ and $\angle 7$

 $\angle 4$ and $\angle 8$

If $l_1 || l_2$, then these corresponding angles are equal in measure; thus:

m∠1 = m∠5

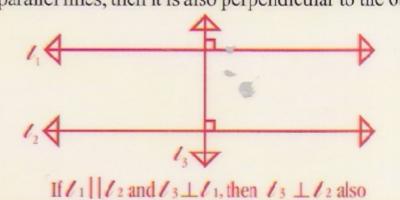
 $m\angle 2 = m\angle 6$

 $m\angle 3 = m\angle 7$ $m\angle 4 = m\angle 8$

Postulate: If the lines are parallel, then the corresponding angles are equal in measure, and if the corresponding angles are equal in measure, then the lines are parallel

7. Right angles (90°) are formed when a transversal is perpendicular to the lines that it intersects

Theorem: If a transversal is perpendicular to 1 of 2 parallel lines, then it is also perpendicular to the other



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Author: Dr. S. B. Kizlik

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